## Program behaviors




## Structural Testing

- Path coverage criteria
- Logic coverage criteria
- Dataflow coverage criteria
- Mutation testing



## Functional Testing

- Boundary Value Testing
- Equivalence Class Testing
- Decision Table-Based Testing
- Combinatorial Testing
- Grammar-based Testing
- Model-based Testing



## Specification-based Testing



## Representative Values

- Try to select inputs
 that are especially valuable
- Usually by Representative values choosing representatives of equivalence classes that are apt to fail often or not at all

The main steps of a systematic approach to functional program testing
(from Pezze + Young, "Software Testing and Analysis", Chapter 10)

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## Boundary Value Testing

Single-fault assumption - therefore only one boundary value at a time

- Minimum, minimum+I, nominal, maximum-I, maximum
- Robustness testing

Minimum-I, maximum+1

- Generalized - single fault assumption Boundary values for one, nominal values for others
- Worst-case testing All possible combinations





## Equivalence Partitioning

| Input condition | Equivalence classes |
| :---: | :---: |
| range | one valid, two invalid <br> (larger and smaller) |
| specific value | one valid, two invalid <br> (larger and smaller) |
| member of a set | one valid, one invalid |
| boolean | one valid, one invalid |

## Equivalence Partitioning

- Weak equivalence class testing One test per equivalence class per input
- Strong equivalence class testing

All combinations (cartesian product of equivalence classes)

- Robustness testing

Include invalid values

- Combination with boundary value testing Test at boundaries of partitions

How do we choose equivalence classes? The key is to examine input conditions from the spec. Each input condition induces an equivalence class - valid and invalid inputs.

## Decision Table Testing




Each column represents one test case

|  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{a}<\mathrm{b}+\mathrm{c}$ | F | T | T | T | T | T | T | T | T | T | T |
| $b<a+c$ |  | F | T | T | T | T | T | T | T | T | T |
| $c<a+b$ |  |  | F | T | T | T | T | T | T | T | T |
| $\mathrm{a}=\mathrm{b}$ |  |  |  | T | T | T | T | F | F | F | F |
| $a=c$ |  |  |  | T | T | F | F | T | T | F | F |
| $\mathrm{b}=\mathrm{c}$ |  |  |  | T | F | T | F | T | F | T | F |
| Not a triangle | X | X | X |  |  |  |  |  |  |  |  |
| Scalene |  |  |  |  |  |  |  |  |  |  | X |
| Isosceles |  |  |  |  |  |  | X |  | X | X |  |
| Equilateral |  |  |  | X |  |  |  |  |  |  |  |
| Impossible |  |  |  |  | X | X |  | X |  |  |  |

## Decision Tables

- Outcome of decisions are not necessarily binary
- Tables can become huge
- Limited entry tables with N conditions have $2^{\mathrm{N}}$ rules
- Don't care entries reduce the number of explicit rules by implying the existence of non-explicitly stated rules.


```
if (pressure < 10) {
    // do something
    if (volume > 300) {
        // faulty code! BOOM!
    }
    else {
        // good code, no problem
    }
}
else {
    // do something else
}
```

Interactions leading to Failure

Interactions leading to Failure

- Medical device O Browser


Interactions leading to Failure

Interactions leading to Failure

## Interactions leading to Failure



- Maximum interactions for fault triggering for studied applications was 6
This correlates to the number of branch statements
- Reasonable evidence
that maximum interaction strength for fault triggering is relatively small
- If all faults are triggered by the interaction of $t$ or fewer variables
then testing all t -way combinations can provide strong assurance
- Pairwise testing finds about $50 \%$ to $90 \%$ of flaws


## How many tests?



- There are 10 effects, each can be on or off
- All combinations is $2^{10}=1,024$ tests
- What if our budget is too limited for these tests?
- Instead, let's look at all 3-way interactions ...


## How many tests?



- There are ${ }_{3}^{10}=1203$-way interactions
- Naively $120 \times 2^{3}=960$ tests.
- Since we can pack 3 triples into each test, we need no more than 320 tests.
- Each test exercises many triples:



## A Covering Array



- Each test covers 120 3-way combinations
- All 3-way combinations (960) in 13 tests
- Finding covering arrays is NP hard


## Another familiar example



No silver bullet because:
Many values per variable
Need to abstract values
But we can still increase information per test
Plan: flt, flt+hotel, flt+hotel+car From: CONUS, HI, Europe, Asia
To: CONUS, HI, Europe, Asia
Compare: yes, no
Date-type: exact, 1to3, flex
Depart: today, tomorrow, 1yr, Sun, Mon
Return: today, tomorrow, 1yr, Sun, Mon
Adults: 1, 2, 3, 4, 5, 6
Minors: 0, 1, 2, 3, 4, 5
Seniors: $0,1,2,3,4,5$

## A Larger Example

Suppose we have a system with on-off switches:


## How do we test this?

34 switches $=2^{34}=1.7 \times 10^{10}$ possible inputs $=1.7 \times 10^{10}$ tests


## What if we knew no failure involves

 more than 3 switch settings?34 switches $=2^{34}=1.7 \times 10^{10}$ possible inputs $=1.7 \times 10^{10}$ tests If only 3 -way interactions, need only 33 tests For 4-way interactions, need only 85 tests


## Two ways of using combinatorial testing



## Testing Configurations

- Example: app must run on any configuration of OS, browser, protocol, CPU, and DBMS
- Very effective for interoperability testing

| Test | OS | Browser | Protocol | CPU | DBMs |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | XP | IE | $\mathrm{IPv4}$ | Intel | MySQL |
| 2 | XP | Firefox | IPv6 | AMD | Sybase |
| 3 | XP | IE | $\mathrm{IPv6}$ | Intel | Oracle |
| 4 | OS $\times$ | Firefox | IPv4 | AMD | MySQL |
| 5 | OS $\times$ | IE | $\mathrm{IPv4}$ | Intel | Sybase |
| 6 | OS $\times$ | Firefox | IPv4 | Intel | Oracle |
| 7 | RHL | IE | $\mathrm{IPv6}$ | AMD | MySQL |
| 8 | RHL | Firefox | IPv4 | Intel | Sybase |
| 9 | RHL | Firefox | IPv4 | AMD | Oracle |
| 10 | OS $X$ | Firefox | IPv6 | AMD | Oracle |

## Combinatorial testing with existent test suite

1. Use t-way coverage for system configuration values
2. Apply existing tests

| Test case | OS | CPU | Protocol |
| :---: | :---: | :---: | :---: |
| 1 | Windows | Intel | IPv4 |
| 2 | Windows | AMD | IPv6 |
| 3 | Linux | Intel | IPv6 |
| 4 | Linux | AMD | IPv4 |

- Common practice in telecom industry


## Generating Covering Arrays

- Search-based methods:
- Mainly developed by scientists
- Advantages: no restrictions on the input model, and very flexible, e.g., relatively easier to support parameter relations and constraints
- Disadvantages: explicit search takes time, the resulting test sets are not optimal
- Algebraic methods:
- Mainly developed by mathematicians
- Advantages: very fast, and often produces optimal results
- Disadvantages: limited applicability, difficult to support parameter relations and constraints


## IPO Strategy

- Builds a t-way test set in an incremental manner
- A t -way test set is first constructed for the first t parameters,
- Then, the test set is extended to generate a t -way test set for the first $\mathrm{t}+\mathrm{I}$ parameters
- The test set is repeatedly extended for each additional parameter.
- Two steps involved in each extension for a new parameter:
- Horizontal growth: extends each existing test by adding one value of the new parameter
- Vertical growth: adds new tests, if necessary

Strategy In-Parameter-Order
begin
/* for the first $t$ parameters $\mathrm{p} 1, \mathrm{p} 2$, ..., pt*/
$\mathrm{T}:=\{(\mathrm{v} 1, \mathrm{v} 2, \ldots, \mathrm{vt}) \mid \mathrm{v} 1, \mathrm{v} 2, \ldots$, vt are values of p1, p2, ..., pt , respectively\}
if $\mathrm{n}=\mathrm{t}$ then stop;
/* for the remaining parameters */
for parameter $\mathrm{pi}, \mathrm{i}=\mathrm{t}+1, \ldots, \mathrm{n}$ do
begin
/* horizontal growth */
for each test (v1, v2, ..., vi-1) in T do
replace it with (v1, v2, ..., vi-1, vi), where vi is a value of pi /* vertical growth */
while T does not cover all the interactions between pi and
each of p1, p2, ..., pi-1 do
add a new test for $\mathrm{p} 1, \mathrm{p} 2, \ldots, \mathrm{pi}$ to T ;
end
end

## Example

- Consider a system with the following parameters and values:
- parameter A has values AI and A 2
- parameter $B$ has values $B I$ and $B 2$
- parameter C has values $\mathrm{Cl}, \mathrm{C} 2, \mathrm{C} 3$

| A | B | A | B | C | A | B | C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| AI | BI | AI | BI | Cl | AI | B1 | Cl |
| AI | B2 | AI | B2 | C2 | AI | B2 | C2 |
| A2 | BI | A2 | BI | C3 | A2 | B1 | C3 |
| A2 | B2 | A2 | B2 | Cl | A2 | B2 | Cl |
|  |  |  |  |  | A2 | B1 | C2 |
|  |  |  |  |  | AI | B2 | C3 |

## Example

- Testing VoIP software:
- Caller,VoIP server, client
- CallerOS:Windows, Mac
- ServerOS: Linux, Sun,Windows
- CalleeOS:Windows, Mac


## Example

| Caller | Server | Callee |
| :---: | :---: | :---: |
| Win | Lin | Win |
| Win | Sun | Mac |
| Win | Win | Win |
| Mac | Lin | Mac |
| Mac | Sun | Win |
| Mac | Win | Mac |

might find some
I. Pairwise testing protects against pairwise bugs
2. while dramatically reducing the number of
tests to perform compared to testing all combinations, but not necessarily compared to testing just the combinations that matter.
3. which is especially cool because pairwise bugs
might represent the majority of combinatoric bugs
or might not, depending on the actual dependencies among variables in the product.
4. and such bugs are a lot more likely to happen
than ones that only happen with more
variables, or less likely to happen, because user inputs are not uniformly distributed.
5. Plus, you no longer need to create these tests by hand. except for the work of a walyzing the product, selecting variables and values, actually configuring and performing the test, and analyzing the results.

